

Array Antenna Animation

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$$F(r) = A \frac{\text{Exp}[-I k r]}{r}$$
$$f(r, t) = \text{Re}[F(r) \text{Exp}[I \omega t]] = \text{Re}\left[A \frac{\text{Exp}[-I(kr - \omega t)]}{r}\right]$$

$\lambda = 1$ として、

$$kr - \omega t = \frac{2\pi}{\lambda} r - \omega t$$
$$\omega = 2\pi f, T = \frac{1}{f} = \frac{2\pi}{\omega}$$

[$kr - \omega t = k(r - ct) = 2\pi(r - ct)$ と表現することもできる]

a point source

```
n = 1;  
a[1] = 1.; xs[1] = 0.; ys[1] = 0.;
```

2-element array

```
n = 2;  
a[1] = 1.; xs[1] = -2.; ys[1] = 0.;  
a[2] = 1.; xs[2] = 2.; ys[2] = 0.;
```

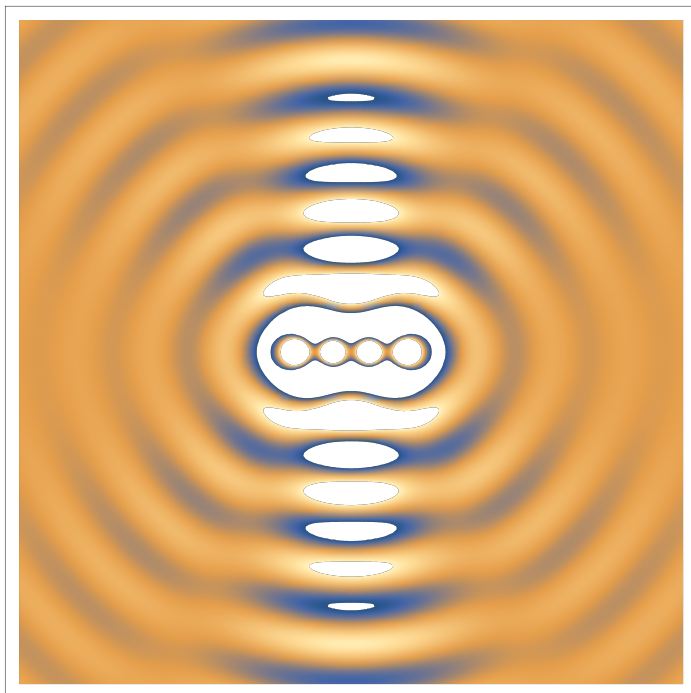
4-element array

```
In[1]:= n = 4;  
a[1] = 1.; xs[1] = 0.; ys[1] = 0.;  
a[2] = 1.; xs[2] = 0.5; ys[2] = 0.;  
a[3] = 1.; xs[3] = 1.0; ys[3] = 0.;  
a[4] = 1.; xs[4] = 1.5; ys[4] = 0.;
```

Graphics and Animation

```
In[6]:=  $\omega = 2 * \pi;$   
 $r[x_, y_, i_] := \sqrt{(x - xs[i])^2 + (y - ys[i])^2};$   
 $Fc[x_, y_] := \text{Sum}[a[i] * \frac{\text{Exp}[-I * 2 * \pi * r[x, y, i]]}{r[x, y, i]}, \{i, 1, n\}]$   
  
 $f[x_, y_, t_] := \text{Re}[Fc[x, y] * \text{Exp}[I * \omega * t]];$   
[実部] [虚数単位]
```

```
In[10]:= DensityPlot[f[x, y, 0], {x, -3.75, 5.25}, {y, -4.5, 4.5},
  密度プロット
  Mesh -> False, PlotPoints -> 100, FrameTicks -> None]
  メ… [偽 [プロットのサンプル点 [枠目盛 [なし
```



```
Table[DensityPlot[f[x, y, t], {x, -3.75, 5.25}, {y, -4.5, 4.5},
  リ… [密度プロット
  Mesh -> False,
  メ… [偽
  PlotPoints -> 20,
  [プロットのサンプル点
  FrameTicks -> None],
  [枠目盛 [なし
  {t, 0, 1 - 0.001, 1/8}]
```